

**UNIVERSITY OF THESSALY**  
**School of Engineering - Department of Civil Engineering**

**Series of Scientific Lectures**  
**Academic Year 2022-2023**

**Nonlinear Waves in Open Channel Flow:**  
**A Dynamical Systems Approach**

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Wednesday **30/11/2022**, Time: **11:15**  
Hybrid Seminar: **Room A1**, [MS Teams](#)  
Live Streaming: [DIAVLOS](#), [YouTube](#)

**Abstract:**

Monoclinal Flood Waves, Undular Bores, Roll Waves and Solitons are among the most iconic *travelling waveforms* observed in Open Channel Flow. On the other side of the spectrum, the Hydraulic Jump, often encountered in open channels, constitutes a paradigmatic example of a *standing waveform*. In this lecture we will show how the generalized Saint-Venant Equations –governing shallow water flow– reduce to a second-order nonlinear Ordinary Differential Equation (ODE) capturing the shape of all standing and travelling waveforms appearing in Open Channel Flow.

To analyze the aforementioned 2<sup>nd</sup>-order ODE we adopt a Dynamical Systems approach, i.e. we treat it as a set of two coupled 1<sup>st</sup>-order ODEs. From this perspective, all travelling waveforms manifest themselves as bounded trajectories in the phase space (local slope vs. local flow depth of a wave) of the dynamical system. The Dynamical Systems approach provides an unprecedented, tangible geometrical insight on the structure of the various waveforms in Open Channel Flow.

